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Compressive Sampling of Color Retinal Image Using Spread Spectrum Fourier Sampling and Total Variant

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ABSTRACT In medical imaging, the application of retinal images demands a lot of retinal photos to analyze and requires efficient compression techniques for retinal image storage. Retinal images must meet stringent quality requirements for clinical data to be accurate and dependable. This paper proposes a compressive sampling (CS) framework for color retinal image (CRI) compression, which relies on spread spectrum Fourier sampling (SSFS) and total variant (TV)-based reconstruction method with three loops of RGB color space, referred to as RGB-TV. In CS, two procedures are performed, i.e., compression and CS reconstruction. In compression steps, SSFS is performed to get a compressed signal from the original CRI with a high compression ratio (CR). While in CS reconstruction, TV-norm and TV proximal operator are exploited for problem optimization to recover original CRI from a compressed signal. In addition, signal-to-noise ratio (SNR), structural similarity (SSIM), and reconstruction time are investigated for the performance metrics of the proposed RGB-TV. The computer simulation result shows that the proposed RGB-TV with a set of CRI of size 512 by 512 pixels can compress until CR = 10 which obtains mean SNR of 22 dB, SSIM 0.84, and reconstruction time of 2.2 seconds.

INDEX TERMS Color retinal image, compressive sampling, RGB, spread spectrum, total variant.

I. INTRODUCTION

For many years, the application of retinal image in medical imaging was studied by researchers, i.e., automatic cataract classification [1], diabetic retinopathy [2], cholesterol level detection [3]–[5], automatic vessel segmentation [6], and retinal prosthesis [7]. These applications demand a lot of retinal images to analyze and require efficient compression techniques for retinal image storage. In addition, because monitoring such retinal images is a complex undertaking, retinal images must meet stringent quality requirements in order for clinical data to be accurate and dependable. This challenge can be mitigated with the use of effective retinal image compression algorithms [8].

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In medical image compression (MIC), various lossy and lossless compression framework were developed. The lossless MICs were proposed, such as a segmentation-based lossless image coding [9], wavelet-based compression scheme [10], adaptive predictive multiplicative autoregressive [11], advanced video coding scheme (H.264/AVC) [12], symmetry-based technique for scalable lossless compression [13], minimum rate predictors [14], and end-to-end optimized learning framework with intra-slice and inter-slice redundancy [15]. In addition, the lossy MICs were developed, i.e., a wavelet-based compression using distortion-constrained adaptive vector quantization [16], optimized volume of interest coding [17], high efficiency video coding [18], and lossy-to-lossless data compression scheme [19]. Moreover, this paper considers a compression framework based on compressive sensing for medical images.

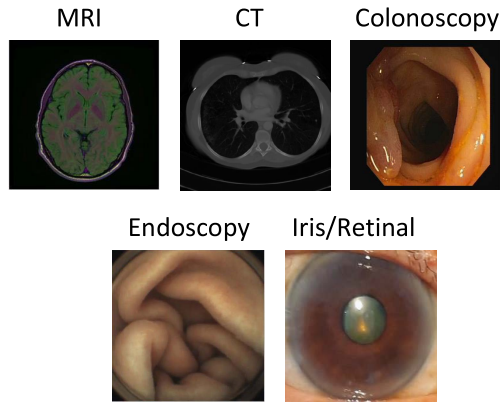


FIGURE 1. An example of medical imaging.

Compressive sampling (CS) was proposed as an approach to sampling a sparse signal with number of sample is less than the Nyquist theorem and the sampled signal can be recovered using a reconstruction method [20]–[22]. Many CS applications in different fields were developed, such as geoscience and remote sensing [23], antennas and wireless propagation [24], signal processing [25], intelligent transportation systems [26], wireless communications [27], and watermarking systems [28], [29]. However, in medical imaging, CS is exploited to speedup the medical investigation time [30].

Recently, an application of CS for MIC using multiple dictionaries of sparse basis was proposed, called compressed medical imaging (CMI) using multi-basis reweighted analysis (M-BRA) [31]. CMI reduces the operational time of medical devices with a sparse acquisition process and stores the samples in the CS domain. This benefit gives less processing time to a patient from medical devices [32]. The transmission, storage, and representation issues in a smaller size with a high perceived quality can also be improved. In [31], four types of medical imaging are considered, i.e., computed tomography, wireless capsule endoscopy images, colonoscopy images, and magnetic resonance imaging. Reference [31] only considers the grayscale format as the input of the proposed CMI. However, color medical images are quite sensitive, need a good quality medical analysis in color feature, and require a CMI in color space (RGB format). Fig. 1 shows an example of medical imaging where colonoscopy, endoscopy, and iris/retinal images are color medical imaging. An initial CMI framework in color medical images considering RGB format was proposed using sparsity averaging (SA) reweighted analysis (RA) and referred to as RGB-SARA [33]. In addition, the CMI of color iris/retinal images using basis pursuit (BP) with SA (RGB-BPSA) [34] was proposed. The previous RGB-based CMI was mostly based on BP where ℓ_1 normalization is exploited for CS reconstruction. To the best of the author's knowledge, total variant (TV)-based CMI for a color medical image is not proposed and investigated yet.

Throughout this paper, a novel TV-based reconstruction method for RGB color retinal images (RGB-TV) is proposed. Different from RGB-SARA [33] and M-BRA [31], RA is not considered in this paper because RA process requires long processing time. This paper aims to reduce the time process and improve the visual quality of CMI. Furthermore, this article presents the CMI contributions as follows

- Novel MIC for a color retinal image is proposed by exploiting CMI to achieve high CR in MIC.
- Novel RGB-based CMI using spread spectrum (SS) Fourier sampling and TV regularization.
- Performance improvement using TV-based CMI and comparison of TV and BP regularization for CS reconstruction.

The rest of this paper is organized as follows. Section II briefly describes the related works. Section III presents CS for compression. In Section IV, the proposed RGB-TV is introduced in detail. Section V presents retinal images, performance metrics, and experiment scenarios. Experiment results are shown in Section VI. Last, Section VII describes the conclusion of this paper.

II. RELATED WORKS

The previous CS framework was proposed using a wavelet-based sparsity basis [20]. Then, a new sparsity basis approach was proposed using the average of multiple sparsity basis prior for radio astronomy images and referred to as sparsity averaging reweighted analysis (SARA) [35]. In addition, an enhanced SARA was proposed by exploiting double concatenated of SARA basis and BP regularization in CS reconstruction of medical imaging, called DC-SARA [36]. Next, a generalized version of DC-SARA was proposed and referred to as M-BRA [31]. However, SARA, DC-SARA, and M-BRA exploit BP for CS reconstruction, while a SARA based on TV was proposed to speedup the reconstruction time of SARA [37]. Last, MIC for the retinal images was proposed by using CS framework based on BP and average sparsity model [34].

III. CS FOR COMPRESSION

In this article, the sparse signal and the compressed signal are denoted by $\mathbf{x}$ and $\mathbf{y}$, respectively. Fig. 2 shows the illustration of CS, i.e., compression and CS reconstruction for color retinal image (CRI).

A. COMPRESSION

In compression, a signal $\mathbf{x} \in \mathbb{C}^{n \times 1}$ is sampled by a sensing matrix $\Phi \in \mathbb{C}^{m \times n}$ to get a compressed signal $\mathbf{y} \in \mathbb{C}^{m \times 1}$ with less m -number of samples. The compression process in CS is defined as

$$\mathbf{y} = \Phi \mathbf{x}. \quad (1)$$

Suppose an CRI is represented by two-dimensional signal I , then I is reshaped to one-dimensional signal $\mathbf{s} \in \mathbb{R}^{n \times 1}$. The requirement of CS as follows, first, if $\mathbf{s}$ is sparse, then $\mathbf{x} = \mathbf{s}$,

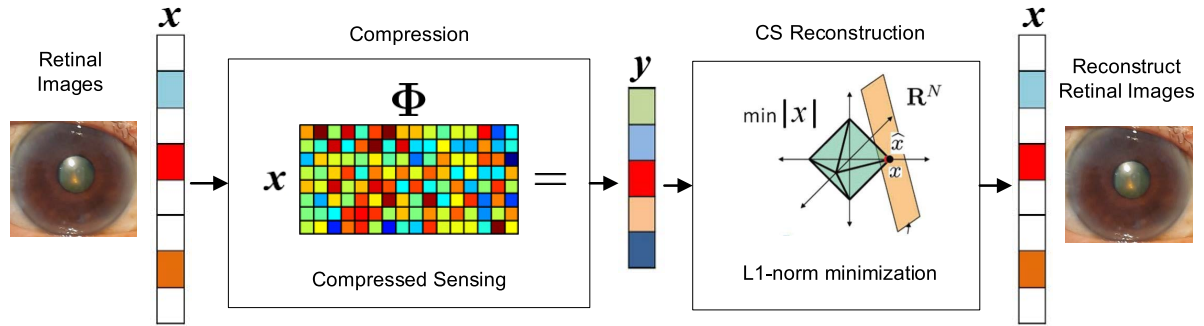


FIGURE 2. An illustration of MIC framework that exploit CS for CRI.

while if s is not sparse, then s is transformed by sparsity basis Ψ to a sparse signal x or $x = \Psi s$. The compression becomes

$$y = \Phi \Psi s, \quad (2)$$

where $\Psi \in \mathbb{C}^{n \times n}$ represents the sparsity basis, $s \in \mathbb{C}^{n \times 1}$ represent the signal, and Φ represents the compression matrix.

B. CS RECONSTRUCTION

In CS reconstruction, a signal reconstructed signal $\hat{x}$ is recovered from y and known Φ and the reconstruction process can be modeled by a convex problem as

$$\min_{\hat{x}} \|\hat{x}\|_1 \quad \text{s. t. } \|y - \Phi \hat{x}\|_2 \leq \varepsilon, \quad (3)$$

where $\hat{x}$, $\|\cdot\|_2$, ℓ_2 norm, ε , and $\|\cdot\|_1$ represent the reconstructed sparse signal, ℓ_2 norm upper bound, and ℓ_1 norm. From Eq. (1), suppose Φ , Ψ , and y are known, then the optimization problem becomes

$$\hat{s} = \min_s \|s\|_1 \quad \text{s. t. } \|y - \Phi \Psi \hat{s}\|_2 \leq \varepsilon. \quad (4)$$

Furthermore, $\hat{I}$ denotes the reconstructed CRI.

C. CS PERFORMANCE METRICS

In CS, compression ratio (CR) is the ratio of x and y as shown in Fig. 2 and defined as

$$\text{CR} = \frac{n}{m}, \quad (5)$$

with n and m are the dimension size of Φ .

The signal to noise ratio (SNR) is calculated from an original image s and a result image $\hat{s}$ and determined as

$$\text{SNR} = \frac{1}{3} \sum_{l=1}^3 10 \log_{10} \left(\frac{\|s_l\|_2}{\|s_l - \hat{s}_l\|_2} \right)^2, \quad (6)$$

where l is each color layer of RGB.

The structural similarity (SSIM) is a perceptual metric that represents the loss of quality in data compression based on contrast, luminance, and structure of the image which are defined as follows

$$\text{con}(s, \hat{s}) = \frac{2\sigma_s \sigma_{\hat{s}} + C_2}{\sigma_s^2 + \sigma_{\hat{s}}^2 + C_2},$$

$$\text{lum}(s, \hat{s}) = \frac{2\mu_s \mu_{\hat{s}} + C_1}{\mu_s^2 + \mu_{\hat{s}}^2 + C_1},$$

$$\text{struc}(s, \hat{s}) = \frac{\sigma_{s\hat{s}} + C_3}{\sigma_s \sigma_{\hat{s}} + C_3}, \quad (7)$$

where σ_s and μ_s denote local standard deviation and mean of the pixel in original CRI. $\sigma_{\hat{s}}$ and $\mu_{\hat{s}}$ denote local standard deviation and mean of the pixel in result image. $\sigma_{s\hat{s}}$ denotes cross-covariance between s and $\hat{s}$. Next, SSIM defined as

$$\text{SSIM}(s, \hat{s}) = [\text{con}(s, \hat{s})]^\beta \cdot [\text{lum}(s, \hat{s})]^\alpha \cdot [\text{struc}(s, \hat{s})]^\gamma. \quad (8)$$

Let C_3 , $C_3 = \frac{C_2}{2}$, and $\alpha = \beta = \gamma = 1$ are assumed as default, SSIM becomes

$$\text{SSIM}(s, \hat{s}) = \frac{(2\mu_s \mu_{\hat{s}} + C_1)(2\sigma_s \sigma_{\hat{s}} + C_2)}{(\mu_s^2 + \mu_{\hat{s}}^2 + C_1)(\sigma_s^2 + \sigma_{\hat{s}}^2 + C_2)}. \quad (9)$$

IV. PROPOSED RGB-TV

Suppose an $N \times N \times 3$ pixels of CRI with RGB format, this paper proposes RGB-TV which is consist of CS and reconstruction as shown in Fig. 3. In CS steps as shown in Fig. 3(a), first, an original CRI is represented by an unsigned integer matrices $I \in \mathbb{Z}^{N \times N \times 3}$, then the original CRI is separated to RGB layer $I_l \in \mathbb{R}^{N \times N}$. Second, RGB loops are performed. For each loop, in SS Fourier sampling, $I_l \in \mathbb{Z}^{N \times N}$ image is reshaped to a signal $x \in \mathbb{R}^{n \times 1}$ with $n = N \times N$ as k -sparse input signal and m sample is measured to obtain measured vector where $k < m < n$ as the CS rule or $0 < \frac{m}{n} < 1$. The RGB loops are finished when all R, G, and B layers are sampled. In reconstruction as shown in Fig. 3(b), a compressed image is reconstructed from the measured vector. Then, RGB loops are performed on each measured vector. TV-based reconstruction is performed for each loop to recover the image from the compressed image. Then, check the condition of the end loop. If the loop is a B layer, the process is finished with the result of RGB images, and the reconstructed image is obtained. While, if the loop is not B layer, then continue to the next loop. Algorithm 1 describes the step of reconstruction.

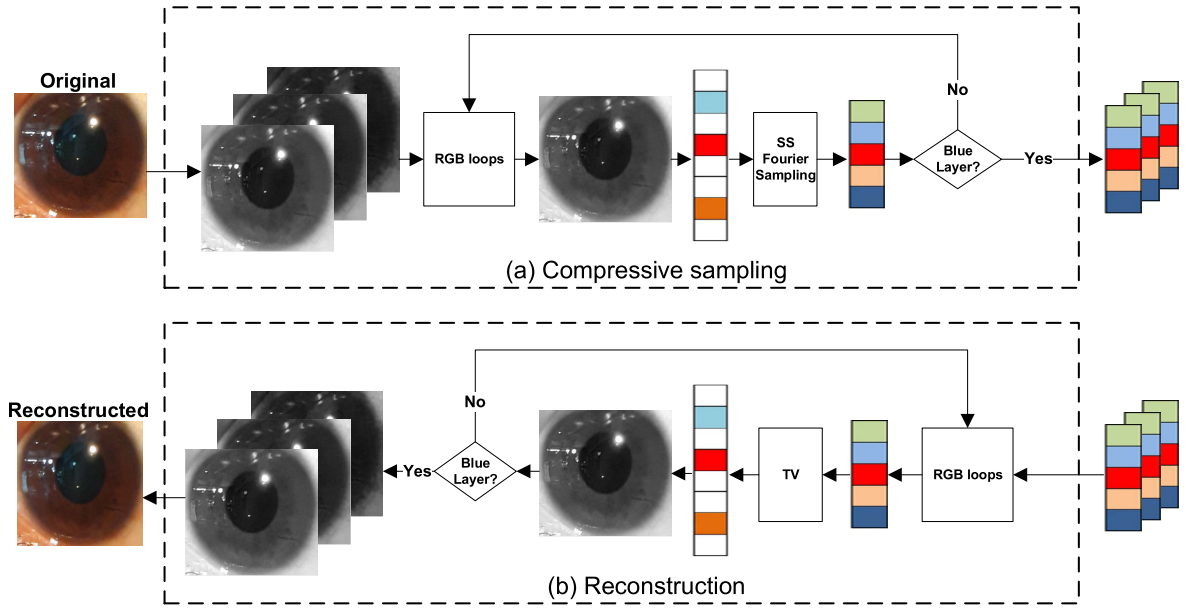


FIGURE 3. The illustration of proposed RGB-TV for CRI compression.

Algorithm 1: RGB-TV

Input: Compressed vector $\mathbf{y} \in \mathbb{R}^{m \times 1 \times 3}$, sampling matrix $\Phi \in \mathbb{R}^{m \times n}$, and ε

Output: The reconstructed CRI $\hat{\mathbf{s}} \in \mathbb{Z}^{N \times N \times 3}$

for $l \leftarrow 1$ **to** 3 **do**

Initialization $t = 1$;

while $t < t_{max}$ and $\alpha > \varepsilon$ **do**

Compute the projection onto the L_2 -ball

$\min_{\hat{\mathbf{x}}} \|\mathbf{x} - \hat{\mathbf{x}}\|_2^2$ s.t. $\|\mathbf{y} - \Phi\hat{\mathbf{x}}\|_2 \leq \varepsilon$;

Compute TV norm $\|\hat{\mathbf{x}}\|_{TV}$;

Compute the TV proximal operator

$\min_{\hat{\mathbf{x}}} \|\mathbf{x} - \hat{\mathbf{x}}\|_2^2 + \lambda \|\hat{\mathbf{x}}\|_{TV}$;

Update $\alpha = \frac{\|\hat{\mathbf{x}}^{(t)} - \hat{\mathbf{x}}^{(t-1)}\|_{TV}}{\|\hat{\mathbf{x}}^{(t-1)}\|_{TV}}$;

$t \leftarrow t + 1$;

end

$\hat{\mathbf{s}}_l = \hat{\mathbf{x}}$;

end

A. SSFS

SSFS is a process to sample a CRI to get compressed signal using a masking matrix (denoted as $\mathbf{M}$) and spectrum matrix (denoted as $\mathbf{A}$) in a domain of discrete Fourier transform matrix (denoted as $\mathbf{F}$). The SSFS is a CS using $\Phi = \mathbf{MFA}$, where $\mathbf{M} \in \mathbb{R}^{m \times n}$ is a rectangular binary matrix, $\mathbf{F} \in \mathbb{C}^{n \times n}$ is a complex matrix, and $\mathbf{A} \in \mathbb{R}^{n \times n}$ is a diagonal matrix. In addition, $\mathbf{MFA}$ can be the inverse transformed that considers $\mathbf{1}_M \in \mathbb{R}^M$ and defined as

$$\mathbf{F}^T \mathbf{M}^T \mathbf{1}_M, \quad (10)$$

In SSFS [38], a noise with input signal-to-noise ratio (ISNR) is considered and the CS process becomes

$$\mathbf{y} = \Phi \mathbf{x} + \mathbf{w}, \quad (11)$$

where $\mathbf{w}$ represents the noise and the ISNR is determined as

$$\text{ISNR} = 10 \log_{10} \left(\frac{\|\Phi \mathbf{x}\|_2^2}{\|\mathbf{w}\|_2^2} \right). \quad (12)$$

B. TV RECONSTRUCTION

In reconstruction process, to reconstruct $\mathbf{x}$ according to Φ , the problem of TV proximal operator [39] is defined as

$$\min_{\hat{\mathbf{x}}} \|\mathbf{x} - \hat{\mathbf{x}}\|_2^2 + \lambda \|\hat{\mathbf{x}}\|_{TV}, \quad (13)$$

where $\hat{\mathbf{x}}$ is a reconstructed signal from the TV.

V. EXPERIMENT

This section presents the experiment to investigate the performance of the proposed RGB-TV. First, retinal images are presented. Second, the experiment scenario is presented. Last, hardware and software specifications are elaborated.

A. CRI

In this paper, real CRI data is considered from a patient at TelkomMedika hospital, Bandung, Indonesia. The acquisition was acquired by one expert operator from the high cholesterol patients. The CRI data consists of 90 images with *.bmp format, RGB colored channel, 660×603 pixels, and 8-bit pixel depth. Furthermore, to make a fair comparison of different CMI methods, $N \times N$ with $N = 64, 128, 256, 512$ are investigated in this paper.

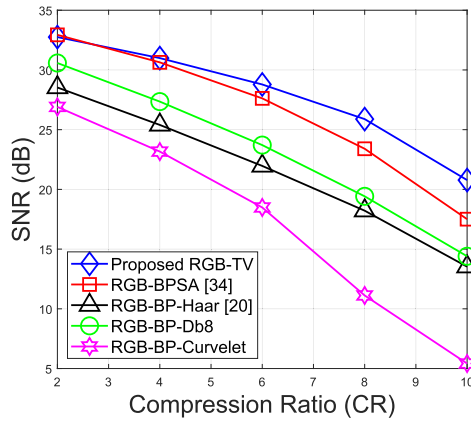


FIGURE 4. The effect of CR to SNR.

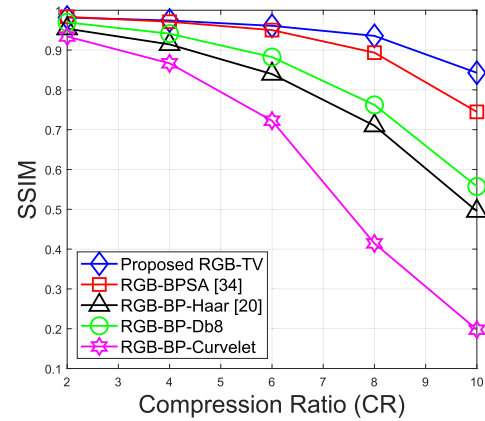


FIGURE 5. The effect of CR to SSIM.

B. EXPERIMENT SCENARIO

This section presents the experiment scenario, first, an $N \times N$ pixels of CRI is considered as the original image. Second, CS is performed according to CR for CRI compression to get a compressed vector. Third, reconstruction is performed by using RGB-TV as presented in Algorithm 1 to recover the reconstructed image from a compressed vector. Last, performance metrics are calculated to investigate the original and reconstructed CRI. Furthermore, the effect of parameters are presented as follows

- Performance metrics with regards to CR, where $N = 64$ is considered as fixed resolution and the different CRs are investigated.
- Performance metrics with regards to ISNR, where $N = 64$ is considered as fixed resolution, $CR = 0.5$ is considered, and ISNR is investigated.
- Performance metrics with regards to N , where 128×128 , 256×256 , and 512×512 pixels are investigated.

This paper compares RGB-TV, RGB-BPSA [34], RGB BP with state-of-the-arts with Haar basis [20], Daubechies 8 (Db8) basis, and curvelet basis. The RGB-TV for CRI is implemented using MATLAB R2020b in a personal computer with a processor 3.20GHz Intel(R) Core(TM) i-8700 CPU and 16GB memory. These specifications are required to validate the processing time results to make a fair comparison with other CMI methods.

VI. EXPERIMENT RESULTS

This section presents the experimental results to validate the scenario and performance metrics presented in Section V-B. The comparison of proposed RGB-TV, RGB-BPSA [34], RGB-BP with state-of-the-arts with Haar basis [20], Daubechies 8 (Db8) basis, and curvelet basis are presented.

A. COMPRESSION RATIO (CR)

Fig. 4 shows the effect of CR to SNR results of proposed RGB-TV, RGB-BPSA [34], RGB-BP-Haar [20], RGB-BP-Db8, and RGB-BP-Curvelet. X and Y-value refer

to $CR = 2, 4, 6, 8, 10$ and SNR in dB, respectively. The results show that the proposed RGB-TV outperforms all CS benchmarks. Targeting $SNR > 20$ dB, RGB-TV achieves at all CR conditions while RGB-BPSA achieves $CR \leq 9$. In addition, the result of RGB-TV and RGB-BPSA at $CR = 2$ are obtained as similar SNR results, then detailed results of SNR are presented in Table 1 and Fig. 6. The box-plot results of SNR with $CR = 2, 4$, and 6 are shown in Fig. 6(a), (b), and (c), respectively. The SNR results in box-plot graphs show that the proposed RGB-TV outperforms all CMIs at $CR = 4$ and 6 with the highest median value of SNR as shown in solid red lines. The median value of RGB-TV at $CR = 2$ is lower than RGB-BPSA but the minimum value of RGB-TV is higher than RGB-BPSA. From Fig. 6, it is validated that RGB-TV outperforms RGB-BPSA at higher CR and more convergence than RGB-BPSA. The same trends are also presented in Table 1 where the mean SNR of the proposed RGB-TV is the best result at all CR conditions.

Next, Fig. 5 shows the results to investigate the SSIM of RGB-TV with regards to $CR = 2, 4, 6, 8, 10$. X-value corresponds to CR and Y-value corresponds to SSIM. The results show that the proposed RGB-TV outperforms all benchmark CMIs. Suppose to aim $SSIM > 0.8$, the proposed RGB-TV achieves at $CR \leq 10$ while RGB-BPSA achieves at $CR \leq 9$. A detailed results of SSIM at $CR \leq 6$ are presented in Table 2 and Fig. 7 to show the difference of the proposed and BPSA results at $CR \leq 6$. The boxplot results of SSIM with $CR = 2, 4$, and 6 are shown in Fig. 7(a), (b), and (c), respectively. The SSIM results in boxplot graphs show that the proposed RGB-TV outperforms all CMIs at $CR = 4$ and 6 with the highest median value of SSIM as shown in solid red lines. The median value of RGB-TV at $CR = 2$ is lower than RGB-BPSA but the maximum value of RGB-TV is higher than RGB-BPSA. From Fig. 7, it is validated that RGB-TV achieved better visual than RGB-BPSA at higher CR and more convergence than RGB-BPSA. In addition, Table 1 shows that the proposed RGB-TV is the best SSIM results

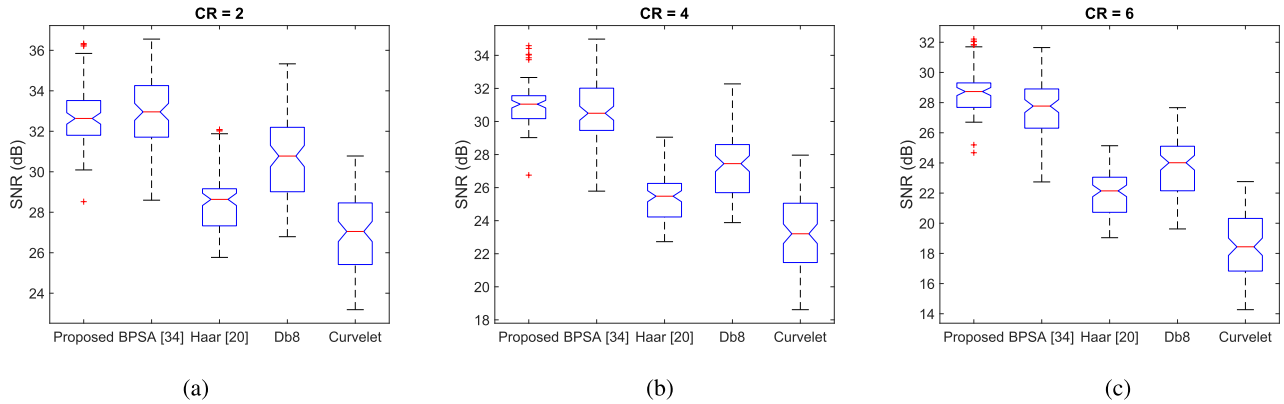


FIGURE 6. Boxplot of ASNR results at $CR \leq 6$.

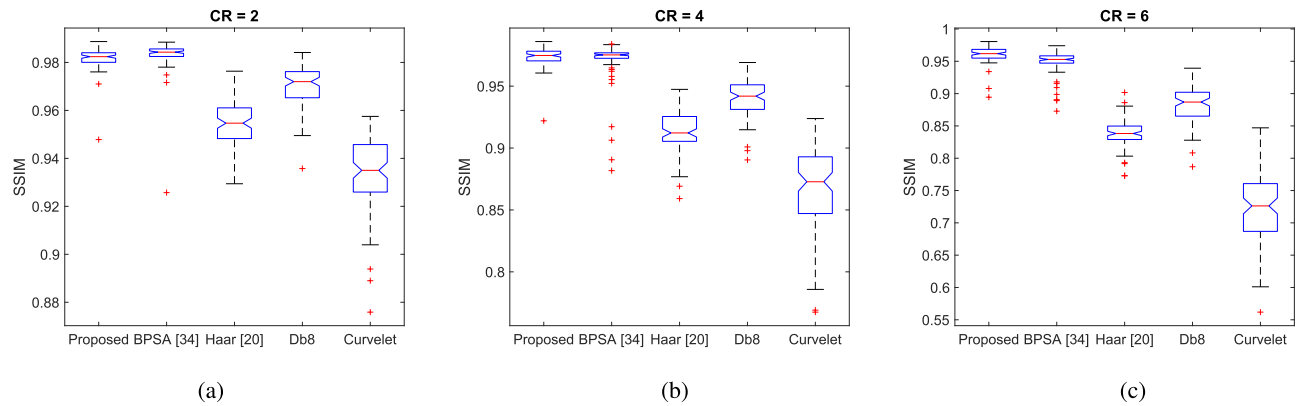


FIGURE 7. Boxplot of SSIM results at $CR \leq 6$ for proposed and BPSA.

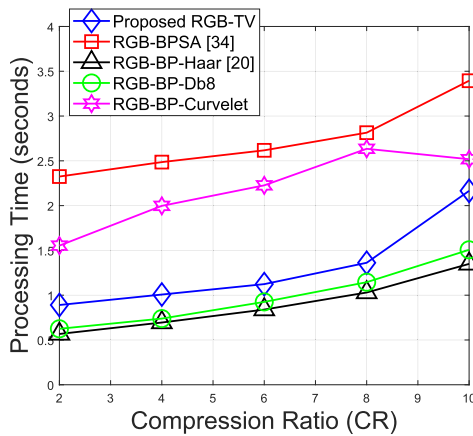


FIGURE 8. The effect of CR to processing time.

at $CR > 4$ with a higher mean SSIM and lower standard deviation.

Last, Fig. 8 shows processing results to analyze the performance of the proposed RGB-TV, RGB-BPSA, RGB-BP-Haar, RGB-BP-DB8, and RGB-BP-Curvelet. The fastest processing time result is RGB-BP-Haar but

TABLE 1. Mean and standard deviation of Fig. 4 at $CR \leq 6$.

	CR = 2	CR = 4	CR = 6
Proposed	32.75 ± 0.40	30.99 ± 0.27	28.78 ± 0.33
BPSA	32.93 ± 0.34	30.63 ± 0.39	27.62 ± 0.12
Haar	28.53 ± 0.12	25.39 ± 0.10	21.96 ± 0.16
Db8	30.58 ± 0.13	27.34 ± 0.12	23.70 ± 0.07
Curvelet	26.90 ± 0.08	23.16 ± 0.07	18.48 ± 0.06

RGB-BP-Haar obtains the second worst SNR and SSIM results. The longest processing time is RGB-BPSA which is achieved ~ 3.4 seconds at $CR = 10$. The processing time of RGB-TV is half times of RGB-BPSA and it is validated that RGB-TV outperforms all CMIs in the view of SNR, SSIM, and processing time.

B. EFFECT OF ISNR

The effect of ISNR on SNR results is shown in Fig. 9(a). Targeting $SNR \geq 30$ dB, both RGB-TV and RGB-BPSA are achieved at $ISNR \geq 23$ dB. It is shown that RGB-TV and RGB-BPSA are obtained similar SNR results, then detailed results of SNR are presented in Fig. 10. The boxplot results of SNR at $ISNR = 10, 30$, and 50 dB are shown in Fig. 10(a), (b), and (c), respectively. For all ISNR conditions, the proposed

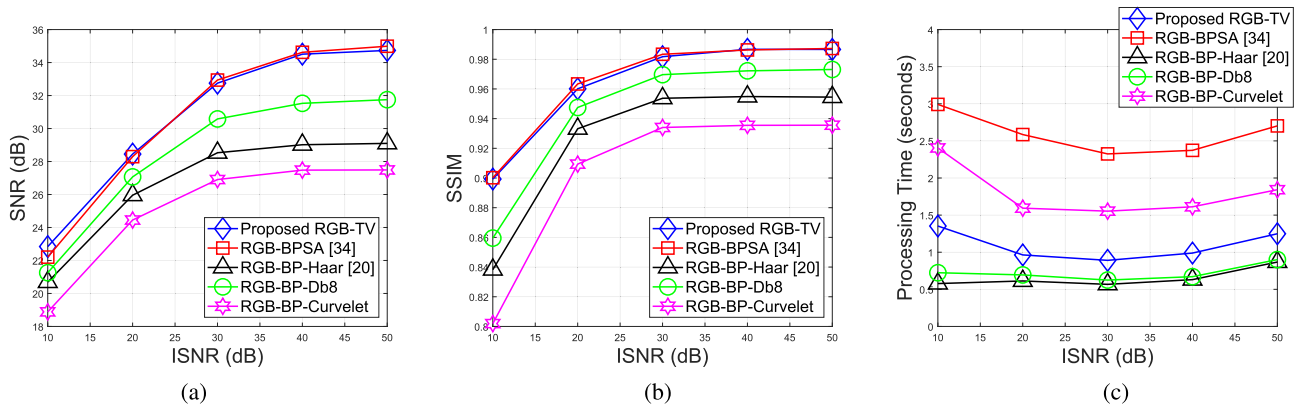


FIGURE 9. Effect of ISNR to performance metrics.

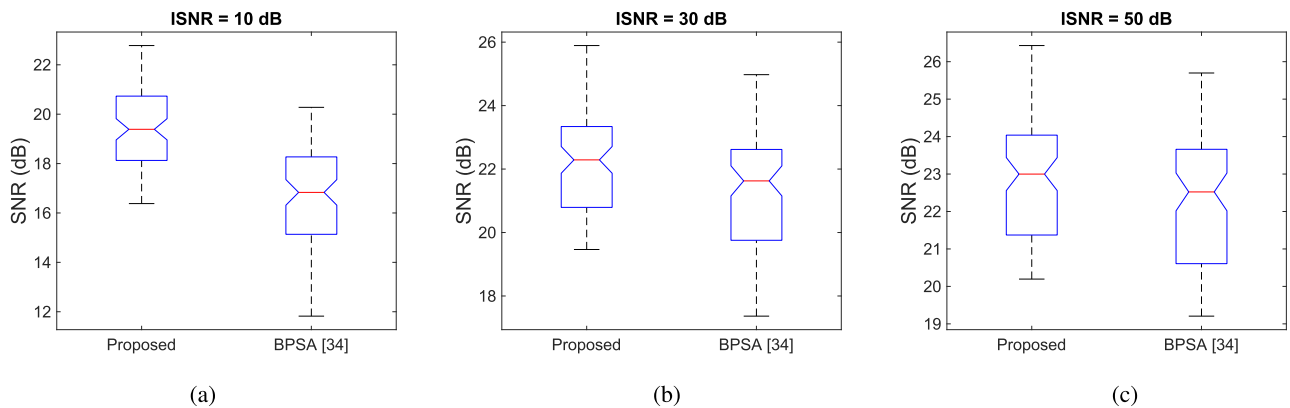


FIGURE 10. Boxplot of ASNR results at ISNR = 10, 30, 50 for proposed and BPSA.

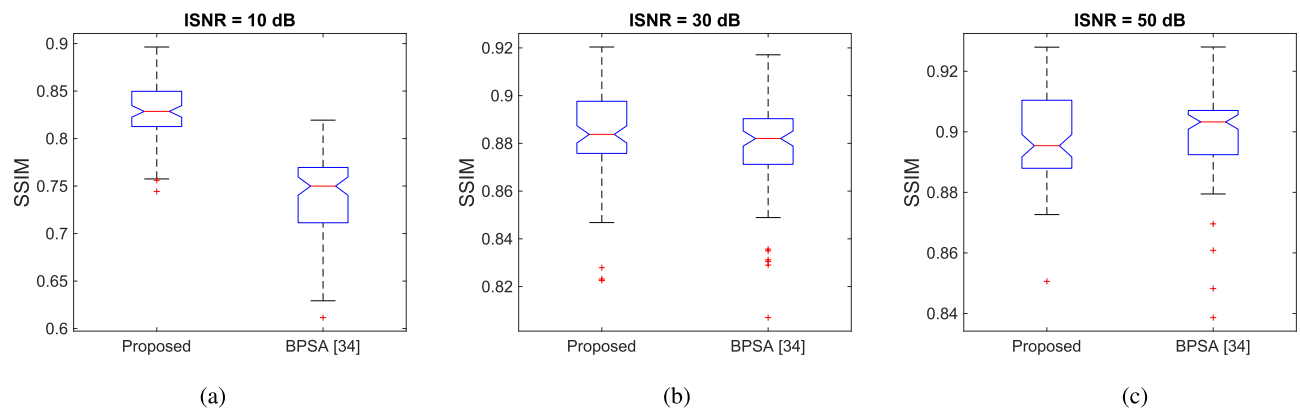


FIGURE 11. Boxplot of SSIM results at ISNR = 10, 30, 50 for proposed and BPSA.

RGB-TV outperforms RGB-BPSA with higher median, minimum, and maximum values in the boxplot results.

The effect of ISNR on SSIM results is shown in Fig. 9(b). Targeting $SSIM \geq 0.98$ dB, both RGB-TV and RGB-BPSA are achieved at $ISNR \geq 30$. The SSIM of RGB-TV and RGB-BPSA are converged around 0.98 at $ISNR \geq 40$. The SSIM of RGB-BP-Db8 is converged around 0.97 at

$ISNR \geq 30$ dB. The SSIM of RGB-BP-Haar is converged around 0.958 at $ISNR \geq 30$ dB, and the SSIM of RGB-BP-Curvelet is converged around 0.937 at $ISNR \geq 30$ dB. It is shown that RGB-TV and RGB-BPSA are obtained similar SSIM results, then detailed results of SSIM are presented in Fig. 11. The boxplot results are presented to show the detailed SSIM results of RGB-TV and RGB-BPSA. The results show

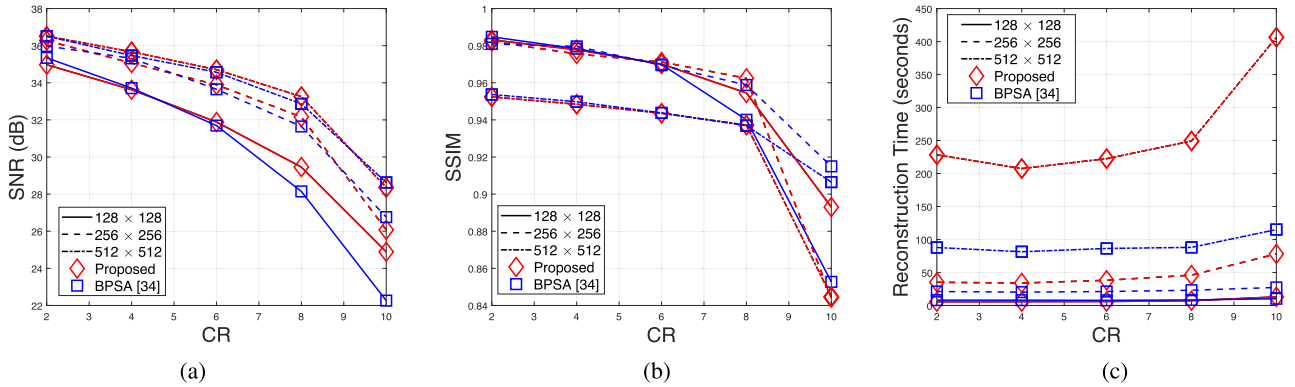


FIGURE 12. Effect of resolutions to performance metrics.

TABLE 2. Mean and standard deviation of Fig. 5 at CR ≤ 6 .

	CR = 2	CR = 4	CR = 6
Proposed	0.981 ± 0.005	0.974 ± 0.007	0.960 ± 0.011
BPSA	0.983 ± 0.008	0.971 ± 0.017	0.950 ± 0.004
Haar	0.953 ± 0.001	0.914 ± 0.002	0.839 ± 0.003
Db8	0.969 ± 0.003	0.941 ± 0.003	0.882 ± 0.003
Curvelet	0.934 ± 0.001	0.866 ± 0.005	0.722 ± 0.004

TABLE 3. The detailed SSIM results of Fig. 9.

ISNR	SNR (dB)		SSIM	
	Proposed	BPSA	Proposed	BPSA
10	22.84 ± 0.09	28.45 ± 0.11	0.910 ± 0.001	0.960 ± 0.002
20	22.20 ± 0.09	28.29 ± 0.15	0.900 ± 0.005	0.963 ± 0.006
30	20.68 ± 0.08	25.95 ± 0.11	0.838 ± 0.001	0.933 ± 0.001
40	21.25 ± 0.09	27.06 ± 0.14	0.859 ± 0.000	0.947 ± 0.000
50	18.88 ± 0.35	24.45 ± 0.22	0.801 ± 0.037	0.909 ± 0.019

that the median value of RGB-TV outperforms RGB-BPSA at ISNR = 10 dB, while RGB-BPSA outperforms RGB-TV at ISNR = 30 and 50 dB. The maximum value of RGB-TV outperforms RGB-BPSA at all ISNR conditions and it is validated that the visual quality result of RGB-TV outperforms RGB-BPSA.

In addition, Table 3 presents the mean and standard deviation results of SSIM concerning ISNR. The results show that RGB-TV outperforms RGB-BPSA at all ISNR conditions with higher mean and lower standard deviation.

Last, Fig. 9(c) shows processing results to analyze the performance of RGB-TV. At all ISNR conditions, RGB-TV and RGB-BPSA are compared, where RGB-TV outperforms RGB-BPSA with less processing time.

C. THE EFFECT OF RESOLUTIONS

Fig. 12(a) shows the effect of resolutions to ASNR. The highest ASNR = 42.53 dB is achieved by 256×256 at CR = 2 while the lowest ASNR = 24.96 dB is achieved by 64×64 at CR = 10. Aiming ASNR > 30 dB, 64×64 attains ASNR ≥ 31.40 dB at CR ≤ 8 , ASNR ≥ 32.22 dB is achieved by 128×128 at CR ≤ 10 , and 256×256 attains ASNR ≥ 37.24 dB at CR ≤ 10 .

Fig. 12(b) shows the effect of resolutions to SSIM. The highest SSIM = 0.9941 is achieved by 245×256 at CR = 2 while the lowest SSIM = 0.8961 is achieved by 64×64 at CR = 10. Aiming SSIM > 0.950, 64×64 attains SSIM ≥ 0.9612 at CR ≤ 8 , SSIM ≥ 0.9612 is attained by 128×128 at CR ≤ 10 , and 256×256 attains SSIM ≥ 0.9846 at CR ≤ 10 .

Fig. 12(c) shows the effect of resolutions to processing time results. The fastest processing time = 4.04 seconds is achieved by 64×64 at CR = 10 while the longest processing time = 44.33 seconds is achieved by 128×128 at CR = 8.

VII. CONCLUSION

This paper proposed a CS framework for compression of a color retinal image using spread spectrum (SS) Fourier sampling and three loops of RGB layers based on TV reconstruction. The proposed CS is referred to as RGB-TV and compared to the recent RGB-BPSA [34]. RGB-TV outperforms the state-the-arts CS using BP (i.e., curvelet, haar, and db8 sparsity basis) and RGB-BPSA. Computer simulation results demonstrated that the proposed RGB-TV achieved better visual quality and faster processing time for CS reconstruction of CRI with a resolution of 64×64 pixels.

For future works, sparse Bayesian learning (SBL) [40] can be considered as a new framework for CMI and an investigation of efficient multitask structure-aware SBL to color retinal images.

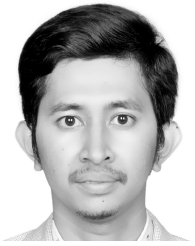
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